

Calculus II, Section 11.1, #22  
Sequences

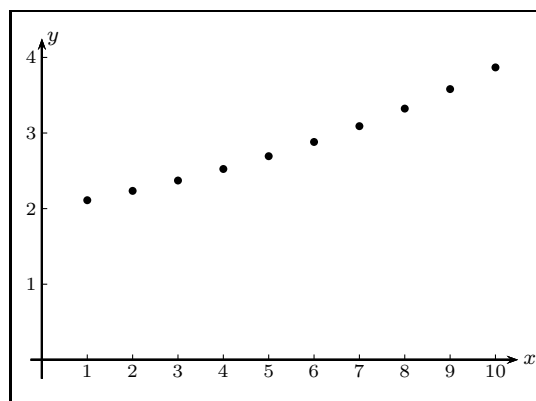
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Calculate, to four decimal places, the first ten terms of the sequence and use them to plot the graph of the sequence by hand. Does the sequence appear to have a limit? If so, calculate it. If not, explain why.<sup>1</sup>

$$a_n = 1 + \frac{10^n}{9^n}$$

The calculated values are shown in the table at left, and are graphed on the right.

$n$	$a_n$
1	2.1111
2	2.2346
3	2.3717
4	2.5242
5	2.6935
6	2.8817
7	3.0908
8	3.3231
9	3.5812
10	3.8680



From the graph, it appears that the sequence does not have a limit.

We can write

$$\begin{aligned} & \lim_{n \rightarrow \infty} \left( 1 + \frac{10^n}{9^n} \right) \\ &= \lim_{n \rightarrow \infty} 1 + \lim_{n \rightarrow \infty} \left( \frac{10}{9} \right)^n \end{aligned}$$

We know the sequence  $\{a_n\}$  is convergent for  $-1 < r \leq 1$  and divergent for all other values of  $r$ . Since  $\frac{10}{9} > 1$ , the sequence  $a_n = 1 + \frac{10^n}{9^n}$  is divergent.

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<sup>1</sup>Stewart, *Calculus, Early Transcendentals*, p. 704, #22.