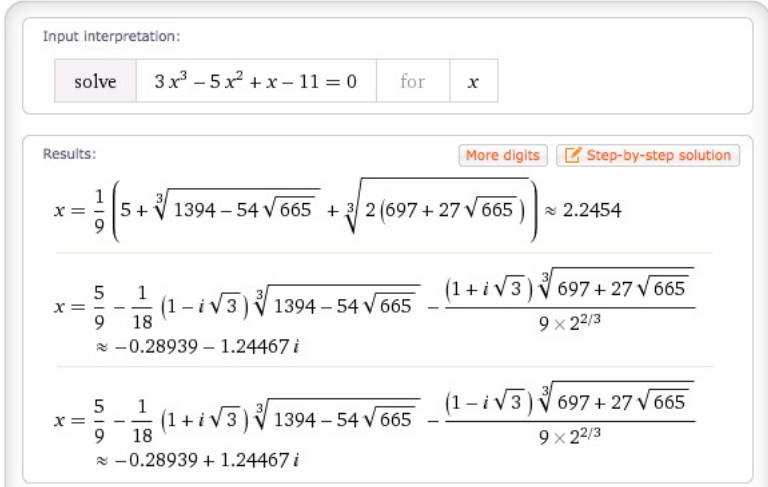


Wolfram|Alpha (W|A) is a free utility available on the Internet. It is published by Wolfram Alpha LLC and was developed by Wolfram Research, Inc.

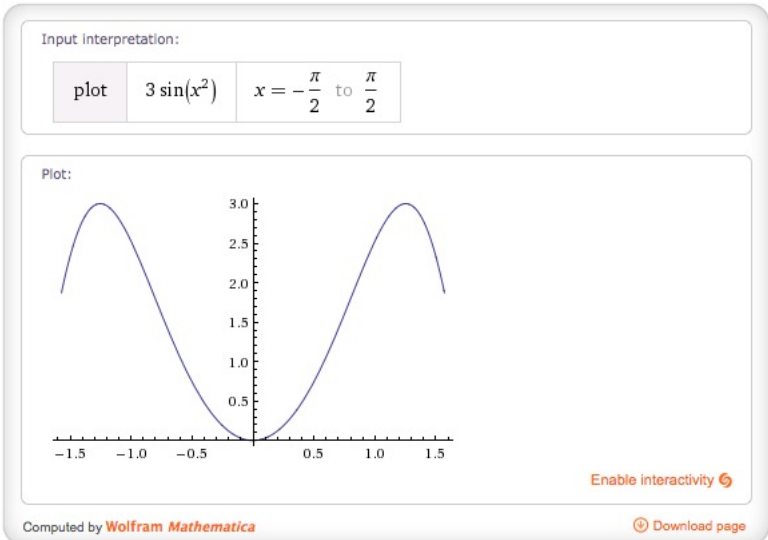


Wolfram|Alpha is one of the most extraordinary utilities on the Internet, and is capable of organizing and delivering a staggering amount of information. However, we are going to focus on its mathematical abilities as they apply to our calculus course.

When asked to perform a mathematical operation, W|A calls on *Mathematica*, a computer algebra system developed by Wolfram Research, Inc. While it is certainly possible to use vernacular language with W|A (indeed, this is one of the most amazing of W|A's abilities) knowing a little of the specific format used by *Mathematica* can help to speed up W|A and to insure that we will get the results that we desire.

Solving Equations

| Traditional | Wolfram Alpha or <i>Mathematica</i> | Comments |
|--|--|--|
| $3x^3 - 5x^2 + x - 11 = 0$ | <code>Solve[3x^3-5x^2+x-11==0, x]</code> | Note the double equal sign for Wolfram Alpha |
|  <p>Input Interpretation:</p> <p>solve $3x^3 - 5x^2 + x - 11 = 0$ for x</p> <p>Results: More digits Step-by-step solution</p> $x = \frac{1}{9} \left(5 + \sqrt[3]{1394 - 54\sqrt{665}} + \sqrt[3]{2(697 + 27\sqrt{665})} \right) \approx 2.2454$ $x = \frac{5}{9} - \frac{1}{18} (1 - i\sqrt{3}) \sqrt[3]{1394 - 54\sqrt{665}} - \frac{(1 + i\sqrt{3}) \sqrt[3]{697 + 27\sqrt{665}}}{9 \times 2^{2/3}} \approx -0.28939 - 1.24467i$ $x = \frac{5}{9} - \frac{1}{18} (1 + i\sqrt{3}) \sqrt[3]{1394 - 54\sqrt{665}} - \frac{(1 - i\sqrt{3}) \sqrt[3]{697 + 27\sqrt{665}}}{9 \times 2^{2/3}} \approx -0.28939 + 1.24467i$ | | |

Graphing Functions

| Traditional | Wolfram Alpha or <i>Mathematica</i> | Comments |
|---|---|---------------------|
| $f(x) = 3 \sin(x^2)$ | <code>Plot[3*Sin[x^2], {x, -Pi/2, Pi/2}]</code> | π is written Pi |
|  <p>Input Interpretation:</p> <p>plot $3 \sin(x^2)$ $x = -\frac{\pi}{2}$ to $\frac{\pi}{2}$</p> <p>Plot:</p> <p>Enable interactivity </p> <p>Computed by Wolfram Mathematica Download page </p> | | |

Differentiation

| Traditional | Wolfram Alpha or <i>Mathematica</i> | Comments |
|---|--|---|
| $\frac{d}{dx} [x^2 - 3x + \ln(2x)]$ | <code>D[x^2 - 3x + Log[2x], x]</code> | For <i>Mathematica</i> , the natural logarithm, $\ln(x)$, is written <code>Log[x]</code> . |
| <div style="border: 1px solid #ccc; padding: 5px;"> <p>Derivative: Step-by-step solution</p> $\frac{d}{dx} (x^2 - 3x + \log(2x)) = 2x + \frac{1}{x} - 3$ <p style="text-align: right; font-size: small;">log(x) is the natural logarithm »</p> </div> | | |
| $\frac{d^4}{dx^4} [e^{x^2} \cos(3x)]$ | <code>D[E^(x^2)*Cos[3x], {x,4}]</code> | For <i>Mathematica</i> , the natural exponential base, e , is written <code>E</code> . Note the computation of the fourth derivative. |
| <div style="border: 1px solid #ccc; padding: 5px;"> <p>Derivative:</p> $\frac{d^4}{dx^4} (e^{x^2} \cos(3x)) = e^{x^2} (24x(3 - 4x^2) \sin(3x) + (16x^4 - 168x^2 - 15) \cos(3x))$ <p style="text-align: right; font-size: small;">Open code ↗</p> </div> | | |
| $\frac{d}{dx} [\sin(xy) = 2x + 3y^2]$ | <code>D[Sin[x*y] == 2x+3y^2, x]</code> | Implicit differentiation; note that xy must be written as <code>x*y</code> . |
| <div style="border: 1px solid #ccc; padding: 5px;"> <p>Result: Step-by-step solution</p> $y'(x) = \frac{y \cos(xy) - 2}{6y - x \cos(xy)}$ </div> | | |

Summation

| Traditional | Wolfram Alpha or <i>Mathematica</i> | Comments |
|--|---|--|
| $\sum_{k=2}^9 (5k^2 - 7k + 1)$ | <code>Sum[5k^2-7k+1, {k,2,9}]</code> | The choice of letter for the counter variable is unimportant. Many books use k or i or n . |
| <div style="border: 1px solid #ccc; padding: 5px;"> <p>Sum:</p> $\sum_{k=2}^9 (5k^2 - 7k + 1) = 1120$ </div> | | |
| $\sum_{k=1}^{\infty} \frac{1}{k^2}$ | <code>Sum[1/(k^2), {k, 0, Infinity}]</code> | How about that! |
| <div style="border: 1px solid #ccc; padding: 5px;"> <p>Infinite sum:</p> $\sum_{k=1}^{\infty} \frac{1}{k^2} = \frac{\pi^2}{6}$ </div> | | |

Integration

| Traditional | Wolfram Alpha or <i>Mathematica</i> | Comments |
|--|---|--|
| $\int \frac{2}{3}t^4 - \tan^{-1}(t) dt$ | <code>Integrate[(2/3)t^4 - ArcTan[t], t]</code> | Note how inverse trig. functions are written. |
| <div style="border: 1px solid #ccc; padding: 10px;"> <p style="text-align: right; margin: 0;">Step-by-step solution</p> <p style="margin: 5px 0;">Indefinite integral:</p> $\int \left(\frac{2t^4}{3} - \tan^{-1}(t) \right) dt = \frac{2t^5}{15} + \frac{1}{2} \log(t^2 + 1) - t \tan^{-1}(t) + \text{constant}$ <p style="margin: 5px 0; text-align: right; font-size: small;"> $\tan^{-1}(x)$ is the inverse tangent function » $\log(x)$ is the natural logarithm » </p> </div> | | |
| $\int_0^{\pi/4} \sin^2(x) \cos^3(x) dx$ | <code>Integrate[Sin[x]^2*Cos[x]^3, {x, 0, Pi/4}]</code> | Definite integrals use the list {variable, lower limit, upper limit} |
| <div style="border: 1px solid #ccc; padding: 10px;"> <p style="text-align: right; margin: 0;">More digits</p> <p style="margin: 5px 0;">Definite integral:</p> $\int_0^{\pi/4} \sin^2(x) \cos^3(x) dx = \frac{7}{60\sqrt{2}} \approx 0.0824958$ </div> | | |